
Zero-Field Splitting in Transition Metal Complexes: Ab Initio Calculations, Effective Hamiltonians, Model Hamiltonians, and Crystal-Field Models

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Introduction

Zero-field splitting (ZFS) is a concept that is commonly used to indicate the loss of the degeneracy of the spin components of a spin-orbit free (SOF) state in the absence of an external magnetic field. This picture of ZFS is based on the separation of SOF and spin-dependent effects such as spin-orbit coupling (SOC). With this viewpoint, ZFS between the spin components of $S > 1/2$ SOF states can be observed in mononuclear complexes (i.e., complexes with one transition metal (TM) center), when (i) the “crystal” field felt by the TM ion is anisotropic (i.e., does not correspond to a spherical or cubic symmetry) and (ii) when SOC is sufficiently large [56]. Spin-spin coupling (SSC) is also at play [55], but usually to a lesser extent. ZFS can in principle occur in any type of systems; however, it is commonly associated with an orbitally nondegenerate ground SOF state. This chapter focuses on TM complexes and more particularly the $3d$ ones. Mononuclear and binuclear (i.e., with two TM centers) complexes will be considered to introduce the main features of single-ion and molecular or intersite anisotropies.

Although ZFS is a concept that has been known for almost a century, it has triggered new investigations in the last 20 years, among which theoretical studies play a key role. One of the reasons for this revival is the discovery of the single-molecule magnet (SMM) behavior [26], which was first evidenced in the so-called Mn_{12} molecule [13]. In this system, the low-temperature magnetic behavior is interpreted as coming from the splitting of the spin components of the $S = 10$ SOF ground state. The slow relaxation of the magnetization from the $M_S = -10$ to $M_S = 10$ components and vice versa is observable at reasonable experimental timescales. The relaxation occurs via different mechanisms, such as thermal activation, direct tunneling, or thermally assisted tunneling. More information concerning SMMs can be, for instance, found in the nice review of Gatteschi and Sessoli [26]. Let us just recall that in order to design higher-temperature SMMs, various strategies have been attempted, as, for instance, enlarging the number of TM centers or enlarging the single-ion anisotropies. More particularly for the latter strategy, it became clear that more extensive studies were necessary to understand the properties of “exotic” coordination spheres with pentacoordinated or heptacoordinated metal centers [16, 68, 75, 76] or even low-coordinated cases [7, 89]. Moreover, the search for magneto-structural correlations from *ab initio* calculations and crystal-field models appeared necessary to eventually guide the synthesis of new coordination complexes, as highlighted by Telsler in 2006 [83].

ZFS also plays an important role in the magnetic properties of condensed matter, as, for instance, ionic solids. In these systems, TM centers may be the subjects of local and intersite anisotropies. Low-temperature magnetic properties of extended systems are at least partly driven by the microscopic interactions that lead to ZFS. One may quote magnetic multiferroics [23], for which magnetic and, for instance, electric transitions are coupled, meaning that one can in principle influence the magnetism of the material by the application of an external electric field or the electric polarization by a magnetic field. One common way of tackling the properties

of solids is to treat infinite systems by applying periodic boundary conditions (PBCs), i.e., neglecting edge effects and assuming an ideally ordered arrangement of the atoms. However, for reasons that will be discussed later in this chapter, it is practically impossible to accurately compute ZFS when PBCs are considered. Another approach, which is perfectly suited for the computation of local effects in ionic solids, consists of using an embedded cluster to model the material, as was done by Pradipto et al. to study cupric oxide [67] and Maurice et al. for LiCu_2O_2 [52]. The interested reader may consult more literature concerning this approach ([33, 34] and references therein), but we already stress that the methods and conclusions that are given in this chapter are directly applicable to solids provided that an embedded cluster approach is followed.

ZFS is often described in terms of model Hamiltonians, which have been (almost) always introduced phenomenologically. Such models are typically spin Hamiltonians, since by definition ZFS applies to systems for which the ground orbital configuration is separated in energy from the others, and hence, the effective description of the lowest-lying states can be restricted to the spin variables. For mononuclear complexes, these Hamiltonians only consider the spin anisotropy of the magnetic center. For polynuclear complexes, two main types of models are widely used, namely, the giant-spin and the multispin models. Both types will be discussed here for binuclear systems to keep the discussion as clear as possible.

This chapter aims at (i) making a bridge between ab initio calculations and model Hamiltonians to validate phenomenological Hamiltonians, (ii) establishing magneto-structural correlations, and (iii) demonstrating that magneto-structural correlations can also be understood in terms of crystal-field models. Therefore, in principle, one can bridge ab initio calculations, model Hamiltonians, and crystal-field models to get a full and intuitive picture of the ZFS in TM complexes. The chapter is organized as follows; first, we describe the ab initio methodologies that are sufficiently accurate to compute ZFS, as well as the effective Hamiltonian theory; second, we discuss the relevance of standard and improved model Hamiltonians that effectively describe the ZFS in mononuclear and binuclear complexes; third, we evaluate magneto-structural correlations, either derived from ab initio calculations performed on model complexes or analyzed within crystal-field model; finally, we conclude on the overall progress made in the last two decades and also give some perspectives.

Ab Initio Calculations and Effective Hamiltonians

In this part, we describe a common strategy to introduce relativistic effects in the calculation of ZFS, the typical way to introduce electron correlation in contracted spin-orbit configuration interaction (c-SOCI) and a way to bridge the resulting spin-orbit wave functions to model Hamiltonians to (i) assess the validity of model Hamiltonians and (ii) extract the model parameter values if appropriate. Apart from the here-discussed approach, other methods have been developed to compute ZFS

and extract the model parameter values [6, 15, 25, 61–63, 66, 78], but these are out of the scope of this chapter.

From the Dirac Equation to Contracted Spin-Orbit Configuration Interaction

The time-independent Dirac equation may be written as:

$$\hat{H}\psi = \left(c \hat{p} \hat{\alpha} + m_e c^2 \hat{\beta} + \hat{V} \right) \psi = E \psi$$

where c is the speed of light, \hat{p} is the momentum operator, $\hat{\alpha}$ and $\hat{\beta}$ are the Dirac 4×4 matrices, \hat{V} is the one-electron external potential, and ψ is a four-component ($4c$) wave function. The resolution of the Dirac equation leads to two different types of solutions; the upper energy eigenfunctions are usually referred to as the “large” components, and the lower energy ones are known as the “small” components. Since the large components tend to standard spin orbitals in the nonrelativistic limit, these may also be considered as “essentially electronic” solutions. Although the introduction of relativistic effects is in principle more natural in $4c$ frameworks, much effort has been devoted in the last decades to reduce the complexity and derive accurate two-component ($2c$) models.

Various transformations/approximations have been implemented in standard codes, among which we quote the Douglas-Kroll (DK) transformation-based expansions [20, 31, 36] and the zeroth-order regular approximation (ZORA) approach [86, 87]. More recently, exact $2c$ formalisms (X2C) have been proposed [35]. Since many investigations of ZFS in TM complexes make use of the DK transformation, we will here describe briefly how to reach c-SOCI formalisms after this transformation, although c-SOCI schemes may also be derived from other reference $2c$ Hamiltonians.

The DK transformation can in principle lead to the exact energies of the Dirac Hamiltonian if one considers an infinite-order expansion of the one-electron external potential (\hat{V}). In practice, the expansion is of course limited to finite order; in most cases, the expansion only contains second-order terms. After the sign correction by Jansen and Hess in the original derivation of the transformation [36], the second-order (and higher) DK expansions are commonly referred to as the Douglas-Kroll-Hess (DKH n) Hamiltonians, where n is the expansion order. Another approximation, called the no-pair transformation, can be then introduced, in which the one-electron kinetic Hamiltonian matrix is diagonalized within a (finite) basis set to form a conventional one-electron basis. Although one can in principle use transformed one-electron and two-electron interactions, a one-component ($1c$) pseudo-relativistic Hamiltonian can be used in scalar relativistic calculations if only the spin-independent one-electron interactions are transformed [72], which means that nonrelativistic two-electron interactions are formally considered. A standard approximation consists of introducing the SOC after a nonrelativistic or scalar

relativistic calculation. Assuming that a set of scalar relativistic reference states has been built in the first step, a c-SOCI calculation consists of diagonalizing $\hat{H} = E_{el} + \hat{H}_{SOC}$ within the basis of the spin components of these reference SOF states, in which E_{el} are SOF electronic energies and \hat{H}_{SOC} is an appropriate SOC Hamiltonian. More details concerning the choice of the SOF electronic energies will be given in the next section. Let us just mention that it is common practice nowadays to use electronic *energies* coming from a higher level of theory than the one that is used to compute the multireference *wave functions*. So in addition to using the reference wave functions for the off-diagonal SOC matrix elements of \hat{H} , one can “dress” the diagonal elements of a c-SOCI matrix with higher-level electronic energies. Such an approach was proposed by [82] and also Llusar et al. [42].

Due to the local character of the spin-orbit operator, one may neglect interatomic SOCs. Expressions for the atomic SOC Hamiltonian that include one-electron and two-electron interactions adapted to the no-pair DKH2 Hamiltonian can be found elsewhere [72]. If one further applies a mean-field approximation to treat the two-electron part of the atomic SOC Hamiltonian by assuming an atomic one-electron density and adding the resulting mean-fields to the one-electron integrals, the so-called atomic mean-field integral (AMFI) approximation is used [32]. Note that alternative mean-field approximations of the SOC operator have been proposed by Neese [60] and that the atomic approximation can nowadays be avoided even in routine calculations.

The Treatment of the Spin-Orbit Free Electron Correlation

Although c-SOCI calculations can in principle be performed using single-reference SOF states, this is not an optimal approach to compute ZFS since it is in most cases impossible to converge enough excited SOF states to obtain a good representation of the SOC operator. Therefore, it is more appropriate to use multireference SOF states, which are obtained from multiconfigurational self-consistent field (MCSCF) approaches. A second requirement to compute ZFS is that all the spin components of the SOF state(s) of interest have to be coupled to excited components in a balanced way, i.e., one should not introduce a bias in the treatment of the lowest-energy spin-orbit states toward one specific spin-orbit component. This common-sense requirement has two implications in practice; (i) the set of SOF states considered in the first step of the calculation must be rather well thought, since selections based on an energy basis do not always lead to a consistent choice, and (ii) it is convenient to consider state-averaged (SA) orbitals between all the SOF states of interest to control the balance between the SOC excitations that are introduced a posteriori. Although SA orbitals can be calculated for any type of MCSCF multireference SOF states, the appropriate calculation of physical properties requires ensuring some properties of the *wave functions*, which may break down by any space truncation of the CI space that is used for computing the SOF states. This is why most researchers

consider the complete active space self-consistent field (CASSCF) method [73] in the first step of a ZFS calculation.

Perhaps it is necessary at this stage to introduce the example of the nearly octahedral d^8 complexes to illustrate how one can consistently choose balanced active spaces and balanced SOCI spaces, i.e., an adequate set of SOF states in the first step of the calculation. If one only considers the d^8 manifold, ten spin-triplet (10T) and 15 spin-singlet (15S) SOF states can be at maximum consideration. Therefore, the easiest way to define balanced spaces consists of choosing an active space of eight electrons in five orbitals, i.e., a CAS(8/5), and in computing 10T and 15S SOF states with the state-averaged CASSCF (SA-CASSCF) method [71]. Note that it is easier to guess which active spaces and which sets of states can be suitable by looking at the reference, most symmetrical situation, i.e., in the octahedral case. One can for instance think of adding the two orbitals associated to the ligand-to-metal “ σ ” donation or to consider the ground SOF state plus a number of excited states that are consistent with the orbital degeneracies in that symmetry point group (“roots”), leading, for instance, to 4T, 7T, and 2S and 10T and 9S sets of SOF states [44]. In any case, the degeneracy of the first three spin-orbit roots should be strictly maintained in the octahedral situation. When the symmetry is lowered, which is necessary to observe ZFS, one should maintain a balanced treatment of the SOC operator. While it is clear that the active spaces that are consistent for the octahedral situation are transferable to the case of nearly octahedral complexes, the definition of the set of SOF states may be problematic. One can always recommend using the full set of states that can be formed within an 8/5 active space (i.e., 10T and 15S) or check that any of the previously mentioned subsets of it leads to similar averaged occupation numbers for the orbitals from which excitations are formed, i.e., for the three orbitals that correspond to the t_{2g} orbitals in the octahedral case. A similar reasoning can be applied to any d^n configuration near an ideal geometry that leads to orbitally nondegenerate ground states, as, for instance, in nearly tetrahedral d^7 complexes. In this case, the “full” set of spin-orbit free states consists of ten spin-quartet (10Q) and 40 spin-doublet (40D) SOF states, while it is also safe to consider the 4Q and 7Q subsets [44].

Now that the set of SOF states has been defined, the SOC is computed between the spin components (i.e., M_S components) of these states to form the c-SOCI matrix. However, one needs to further discuss the choice of the SOF electronic energies that appear on the diagonal of the matrix. Since the spin components of the SA-CASSCF SOF states are considered to compute the off-diagonal elements of the c-SOCI matrix, it may appear natural to just consider the SA-CASSCF electronic energies on the diagonal of this matrix. This straightforward choice may however not be the wisest. In mononuclear complexes, satisfactory results may be obtained at this level, although it is also clear that results are in general slightly improved when the diagonal of the c-SOCI matrix is “dressed” with post-CASSCF correlated energies [44]. In binuclear complexes, ZFS can be severely underestimated if SA-CASSCF energies are considered on the diagonal elements

of the c -SOC matrix, as shown by Maurice et al. showed in a very detailed study concerning the ZFS of the first excited spin-triplet block in copper acetate monohydrate [50]. In this case, it was shown via a crystal-field model that the ZFS of interest relates at second order of perturbation to the isotropic magnetic couplings of the orbitally single-excited states. As shown by decades of experience, a proper description of isotropic magnetic couplings is not trivial at post-CASSCF levels [43]. Perturbative approaches such as the complete active space perturbation theory at second order (CASPT2) [4] and the n -electron valence state perturbation theory at second order (NEVPT2) [5] do not fully account for the effect of charge-transfer configurations on the isotropic couplings. Although the description is clearly improved compared to CASSCF, multireference configuration interaction (MRCI) has to be considered for quantitative results. Among the different MRCI schemes, the difference-dedicated configuration interaction (DDCI) methods [57] is one of the most successful ones for computing isotropic couplings. This method considers all the single and double excitations minus the double excitations that create two holes (h) in the inactive orbitals and two particles (p) in the virtual orbitals, usually referred to as the $2h2p$ excitations. Numerical examples will be given in sections “[Mononuclear Complexes](#)” and “[Binuclear Complexes](#)” for mononuclear and binuclear complexes, respectively, and the comparison with experimental data will be discussed.

On the Effective Hamiltonian Theory

The effective Hamiltonian theory [8, 18] enables one to establish a bi-univocal relation between a sophisticated Hamiltonian (here called the “reference” Hamiltonian) expressed in a large reference space and an effective Hamiltonian working on a truncated space, usually of much smaller dimension, that is called the “model” space. By definition, the eigenfunctions of an effective Hamiltonian are the wave functions of the reference Hamiltonian projected onto the model space, while its eigenvalues are set to be identical to the energies of the reference Hamiltonian. Note that effective Hamiltonians can be used to design computational approaches [14, 24, 79, 80]. Alternatively, effective Hamiltonians can be used to extract information from wave functions and energies in order to determine the interactions of model Hamiltonians (i.e., the model operators and parameters). By doing so, computational chemistry can (i) assess the validity of the considered model Hamiltonian by checking that the model space is appropriate (the norms of the projections onto the model space must be large enough) and checking that the operators of the model Hamiltonian are the relevant ones (a good one-to-one correspondence between the model Hamiltonian and the effective Hamiltonian matrices must be obtained) and (ii) extract the model parameter values. This approach proved to be particularly appropriate in the field of ZFS for the second purpose, even if alternatives exist, as, for instance, the pseudo-spin approach of Chiboratu and Ungur [15].

Various formulations of effective Hamiltonians have been reported in the literature, among which the [8] and des Cloizeaux [18] ones that will be commented here. The Bloch formulation of the effective Hamiltonian is defined as:

$$\hat{H}_{\text{Bloch}} = \sum_k |\tilde{\psi}_k\rangle E_k \langle S^{-1} \tilde{\psi}_k|$$

where $\tilde{\psi}_k$ and E_k are the k th projected eigenvector and eigenvalue of the reference Hamiltonian. The projected eigenvectors of the reference Hamiltonian are mutually non-orthogonal, and S^{-1} is the inverse of the overlap matrix between the projected eigenvectors. However, one should note that this formulation does not ensure hermiticity of the effective Hamiltonian, which may be problematic for extracting model parameter values. In order to get Hermitian model Hamiltonians, the des Cloizeaux formalism, which symmetrically orthogonalizes the projected eigenvectors (usually referred to as the Löwdin's orthogonalization in quantum chemistry), can be used. In this formalism, the effective Hamiltonian is defined as:

$$\hat{H}_{\text{des Cloizeaux}} = \sum_k \left| S^{-\frac{1}{2}} \tilde{\psi}_k \right\rangle E_k \left\langle S^{-\frac{1}{2}} \tilde{\psi}_k \right|$$

Examples of discussions on the validity of model Hamiltonians and extractions of model parameter values are given in the next section.

Model Hamiltonians and Effective Hamiltonians

Model Hamiltonians not only reduces the complexity of a given reference Hamiltonian, the model space being always smaller than the reference space, but also introduce effective parameters with a well-defined physical meaning. In the field of molecular magnetism, the typical simpler Hamiltonians are the well-known phenomenological spin Hamiltonians, in which no track of the orbital part of the wave functions is kept. Although the earliest spin Hamiltonian is the Heisenberg-Dirac-van Vleck (HDV) [19, 29, 88] one (vide infra), the expression “spin Hamiltonian” was introduced later by Abragam and Pryce [2] in the context of the electron paramagnetic resonance (EPR) spectroscopy. In this part, we will show that (i) the *effective Hamiltonian theory* can be used to project the information contained in c-SOCI wave functions onto a model space consisting of the spin components of one (or several) spin state(s), (ii) question the validity of *model Hamiltonians* and improve them if necessary, and (iii) show that model parameter values in good agreement with experiment can be obtained. We will start by discussing mononuclear complexes prior to dealing with binuclear systems to gradually increase the complexity of the models to be introduced. Note that a basic introduction to the use of effective Hamiltonian theory in relation to model Hamiltonians can be found in a recent textbook [17].

Mononuclear Complexes

Mononuclear complexes with a d^n electronic configuration can be split in two groups, $S = 1$ or $S = 3/2$ systems and $S = 2$ or $S = 5/2$ systems, as the model Hamiltonians that have to be used to describe the full complexity of their ZFS are different. Note that, in a first approximation, the model Hamiltonian for $S = 1$ or $S = 3/2$ systems can be used to describe $S = 2$ or $S = 5/2$ systems. Although this is commonly done in the literature, this approximation may not always be adequate, as will be discussed later. One should also stress that usually, in the $S = 2$ or $S = 5/2$ systems, the SSC can contribute to a significant part of the total ZFS, around 10 % of the total ZFS in manganese(III) complexes [21] and even up to 20 % in manganese(II) complexes [90]. Therefore, one should account for the SSC in the determination of ZFS parameters [61]. A remark is thus worth here. Both SOC and SSC generate second-rank ZFS tensors, and, unless these axes are imposed by symmetry, both effects may independently generate different magnetic axes. Therefore, one should in principle not only perform a c-SOCI calculation but rather diagonalize $\hat{H} = E_{el} + \hat{H}_{SOC} + \hat{H}_{SSC}$ prior to applying the effective Hamiltonian theory. This point is also valid for the $S = 1$ and $S = 3/2$ systems, although \hat{H}_{SSC} can be more safely neglected in these cases, especially in complexes for which large ZFSs are observed. For mononuclear complexes, we compare computed values to experimental ones when the SSC contribution to the ZFS can be neglected. When this contribution is expected to play a more important contribution, we do not compare to experiment but rather focus on the SOC contribution and on the validity of the model Hamiltonians.

$S = 1$ and $S = 3/2$ Systems

For $S = 1$ and $S = 3/2$ systems, the model Hamiltonian which describes the ZFS of orbitally nondegenerate states is simply [39]:

$$\hat{H}_{\text{mod1}} = \hat{S} \overline{\overline{D}} \hat{S}$$

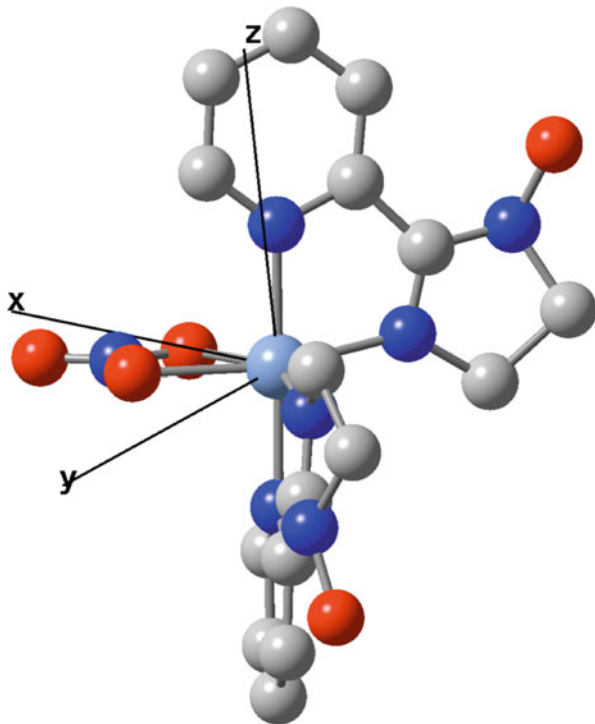
where \hat{S} is the spin operator row or column vector and $\overline{\overline{D}}$ the second-rank ZFS tensor. $\overline{\overline{D}}$ is symmetric and only composed of real numbers. Expanding this Hamiltonian and applying it to the $|S, M_S\rangle$ spin component basis allows one to derive the analytical interaction matrix to be compared to the effective Hamiltonian matrix. Although a similar reasoning can be used for $S = 3/2$ systems, we will only discuss in details the $S = 1$ case. Note that the analytical interaction matrix for $S = 3/2$ systems is available elsewhere [44]. The analytical interaction matrix is given in Table 1 for $S = 1$. As mentioned earlier, the analytical interaction matrix is Hermitian (see Table 1), as any other analytical interaction matrix that will be discussed in this chapter.

The c-SOCI calculation delivers wave functions expressed in terms of the spin components of a set of SOF states. To describe the ZFS of an $S = 1$ system with \hat{H}_{mod1} , the c-SOCI eigenvectors have to be projected onto the

Table 1 Analytical interaction matrix corresponding to the ZFS of $S = 1$ systems [44]. X , Y , and Z correspond to the Cartesian axes of an arbitrary axis frame

$\widehat{H}_{\text{mod1}}$	$ 1, -1\rangle$	$ 1, 0\rangle$	$ 1, 1\rangle$
$\langle 1, -1 $	$\frac{1}{2}(D_{XX} + D_{YY}) + D_{ZZ}$	$-\frac{\sqrt{2}}{2}(D_{XZ} + iD_{YZ})$	$\frac{1}{2}(D_{XX} - D_{YY}) + iD_{XY}$
$\langle 1, 0 $	$-\frac{\sqrt{2}}{2}(D_{XZ} - iD_{YZ})$	$D_{XX} + D_{YY}$	$\frac{\sqrt{2}}{2}(D_{XZ} + iD_{YZ})$
$\langle 1, 1 $	$\frac{1}{2}(D_{XX} - D_{YY}) + iD_{XY}$	$\frac{\sqrt{2}}{2}(D_{XZ} - iD_{YZ})$	$\frac{1}{2}(D_{XX} + D_{YY}) + D_{ZZ}$

Fig. 1 Ball-and-stick representation of a model of the $[\text{Ni}(\text{HIM2-Py})_2\text{NO}_3]^+$ complex and its main magnetic axes [44]. The “external” methyl groups have been modelled by hydrogen atoms; all hydrogen atoms are omitted for clarity



spin components of a SOF state, typically the ground state. The norm of the projection can be assessed by looking at the diagonal elements of the overlap matrix between the projected eigenvectors (S in $\widehat{H}_{\text{Bloch}}$ or in $\widehat{H}_{\text{des Cloizeaux}}$). If the (ground) SOF state is well separated in energy from any other SOF state, the norm of the projections is expected to be close to 1. Let us choose the example of the $[\text{Ni}(\text{HIM2-Py})_2\text{NO}_3]^+$ (HIM2-py = 2-(2-pyridyl)-4,4,5,5-tetramethyl-4,5-dihydro-1H-imidazolyl-1-hydroxy) complex (see Fig. 1) [44].

The projected wave functions are obtained from the ab initio ones simply by truncation, i.e. by only the part that concerns the spin components of the Ψ_0 ground SOF states:

Table 2 Effective interaction matrix corresponding to the ZFS of the $[\text{Ni}(\text{HIM2-Py})_2\text{NO}_3]^+$ complex [44]

$\hat{H}_{\text{des Cloizeaux}}$	$ \Psi_0, -1\rangle$	$ \Psi_0, 0\rangle$	$ \Psi_0, 1\rangle$
$\langle\Psi_0, -1 $	6.386	$-0.690 + i0.376$	$-3.734 + i3.134$
$\langle\Psi_0, 0 $	$-0.690 - i0.376$	0.125	$0.690 - i0.376$
$\langle\Psi_0, 1 $	$-3.734 - i3.134$	$0.690 + i0.376$	6.386

$$|\tilde{\Psi}_1\rangle = (0.045 + i0.092)|\Psi_0, -1\rangle - (0.668 - i0.724)|\Psi_0, 0\rangle$$

$$+ (0.096 + i0.037)|\Psi_0, 1\rangle$$

$$|\tilde{\Psi}_2\rangle = -(0.395 - i0.578)|\Psi_0, -1\rangle + (0.062 + i0.088)|\Psi_0, 0\rangle$$

$$- (0.096 - i0.173)|\Psi_0, 1\rangle$$

$$|\tilde{\Psi}_3\rangle = (0.701 + i0.026)|\Psi_0, -1\rangle - (0.090 + i0.037)|\Psi_0, 0\rangle$$

$$- (0.519 + i0.472)|\Psi_0, 1\rangle$$

The norms of the projected vectors (prior to orthonormalization) are all larger than 0.99, which perfectly legitimates the use of a spin Hamiltonian in this case. However, prior to validating \hat{H}_{mod1} , other tests are necessary: one must show that (i) the effective and analytical interaction matrices match and (ii) how the extracted tensor component values transform with respect to a change of the axis frame (i.e., that the extracted $\overline{\overline{D}}$ actually transforms as a tensor). The effective interaction matrix that is built with $\hat{H}_{\text{des Cloizeaux}}$ is represented in Table 2 ($E_1 = 0.00$, $E_2 = 1.529$ and $E_3 = 11.396$, all energies being in cm^{-1}).

By construction, the effective interaction matrix is Hermitian and has the same eigenvalues as the reference Hamiltonian ($\hat{H}_{\text{ref}} = E_{el} + \hat{H}_{\text{SOC}}$), and its eigenvectors $\tilde{\Psi}_1$, $\tilde{\Psi}_2$, and $\tilde{\Psi}_3$ are identical to the projected ab initio eigenvectors up to a given complex phase factor. By the term-by-term comparison of \hat{H}_{mod1} and $\hat{H}_{\text{des Cloizeaux}}$, it is immediately clear that both matrices perfectly match, meaning that \hat{H}_{mod1} is suited to describe the ZFS in this system, as it turns out to be the case for any $S = 1$ system with an orbitally nondegenerate ground state. Therefore, the second-rank ZFS tensor can be unambiguously extracted. Diagonalization of this tensor leads to the determination of the magnetic axes X^m , Y^m , and Z^m , as well as the ZFS parameters:

$$D = D_{Z^m Z^m} - \frac{1}{2}(D_{X^m X^m} + D_{Y^m Y^m})$$

$$E = \frac{1}{2}(D_{X^m X^m} - D_{Y^m Y^m})$$

provided that conventions are applied, i.e., $|D| > 3E$ and $E > 0$ (or, alternatively $E/D > 0$). If one uses the transformation matrix P^{-1} that allows expressing

$\overline{\overline{D}}$ in the magnetic axis frame (such that $\overline{\overline{D}}^m = P^{-1}\overline{\overline{D}}P$), one can build again $\widehat{H}_{\text{des Cloizeaux}}$ after computing the c-SOCI solutions in this coordinate system and show that the extracted tensor is diagonal and finally that the same ZFS parameters can be extracted. Therefore, we conclude that $\overline{\overline{D}}$ actually transforms as a second-rank tensor and show that the model Hamiltonian $\widehat{H}_{\text{mod1}}$ is fully valid. In this case, the extracted values for D and E are -10.60 and 0.76 cm^{-1} , respectively, [44] and compare well with the most accurate experimental values (-10.15 and 0.10 cm^{-1} , respectively, from high-field and high-frequency EPR spectroscopy [70]). Other nickel(II) complexes have been studied in a similar way, and a good agreement between theory and experiment is generally observed with c-SOCI [16, 44, 51, 75, 76], while density functional theory methods seem to fail for this high-spin d^8 configuration [41].

A similar reasoning can be applied to $S = 3/2$ complexes, such as nearly tetrahedral cobalt(II) complexes. The D and E parameters cannot be extracted from the eigenvalues of any reference Hamiltonian, since one only has access to the energy difference between the two Kramer's doublets of interest. On the contrary, the application of the effective Hamiltonian theory unambiguously allows extracting the full ZFS tensor, i.e., determining the magnetic axes and the ZFS parameters. As shown elsewhere [44], $\widehat{H}_{\text{mod1}}$ is indeed also perfectly suited to describe the ZFS of $S = 3/2$ ground states. As an example of application, let us consider the $[\text{Co}(\text{PPh}_3)_2\text{Cl}_2]$ (Ph = phenyl) complex (see Fig. 2) [44]. In this case, the extracted ZFS parameter values are -14.86 and 0.54 cm^{-1} for D and E , respectively [44], which also compares well to the experimental values of -14.76 and 1.14 cm^{-1} , respectively [40]. Also, note that the energy difference from the two Kramer's doublet of interest relates to the D and E parameters as follows:

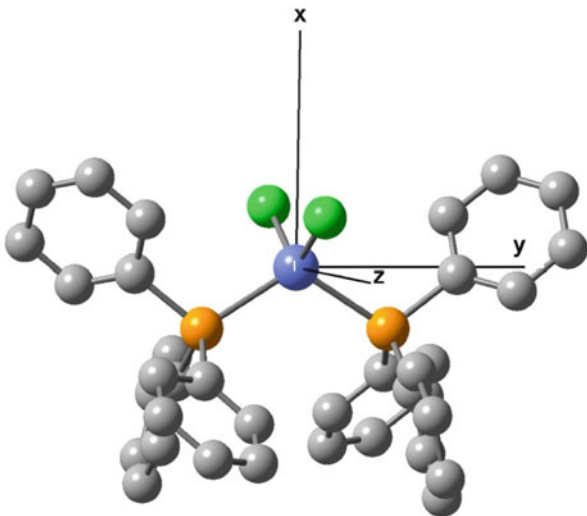
$$\Delta E = 2\sqrt{D^2 + 3E^2}$$

In both nickel(II) and cobalt(II) examples described above, the computational methodology was based on SA-CASSCF calculations with quite large active spaces, small sets of SOF states (4T and 7Q, respectively), and CASPT2 correlated energies [44]. As a recommendation, one may note that enlarging the set of SOF states does not systematically improve the results: on the one hand, more SOC excitations are accounted for, and on the other hand, averaging artifacts are introduced, which may result, for instance, in a poor orbital set for describing the ground state. Therefore, one should make the compromise of describing as best as possible the stronger SOC interactions, i.e., the balance between the number of possible excitations and the accurate description of the involved states. As a conclusion concerning the ab initio methodology, one may say that c-SOCI methods do not constitute a "black-box machinery" to compute ZFSs.

$S = 2$ and $S = 5/2$ Systems

For $S = 2$ and $S = 5/2$ complexes, additional operators must be introduced in the model Hamiltonian to achieve a complete description of the ZFS:

Fig. 2 Ball-and-stick representation of the $[\text{Co}(\text{PPh}_3)_2\text{Cl}_2]$ complex and its main magnetic axes [44]. All the hydrogen atoms are omitted for clarity



$$\hat{H}_{\text{mod}2} = \hat{S} \overline{\overline{D}} \hat{S} + \sum_{q=-4}^4 B_4^q \hat{O}_4^q$$

where q may be odd and where the \hat{O}_4^q operators are extended Stevens operators [1, 3, 77, 81]. This Hamiltonian is valid in any arbitrary axis frame for $S = 2$ and $S = 5/2$ complexes. When the ground SOF state is well separated in energy from the excited states, the fourth-rank spin \hat{O}_4^q operators have a very small effect on the effective interactions of the model $\hat{H}_{\text{mod}1}$. Therefore, one can first find the main anisotropy axes by extracting $\overline{\overline{D}}$ from the comparison of the effective interaction matrix and the analytical one that is obtained with $\hat{H}_{\text{mod}1}$ and then compute the effective interaction matrix in this frame after a second c-SOCI calculation. In this case, the model Hamiltonian reduces to:

$$\hat{H}_{\text{mod}3} = \sum_{n=0}^4 \sum_{k=2}^4 B_k^n \hat{O}_k^n$$

where k and n must be even and the \hat{O}_k^n operators are standard Stevens operators. Note that $B_2^0 = D/3$ and that $B_2^2 = E$, i.e., B_2^0 is a second-rank axial ZFS parameter, while B_2^2 is a rhombic one. As shown elsewhere, this two-step procedure leads to the unambiguous extraction of the main magnetic axes and of the five B_k^n parameters (B_2^0 , B_2^2 , B_4^0 , B_4^2 , and B_4^4) [45]. Indeed, in the magnetic axis frame, the effective interaction matrix is in almost perfect correspondence with the analytical one derived for $\hat{H}_{\text{mod}3}$ with only some negligible deviations, typically not larger than 0.01 cm^{-1} . These deviations can be considered as numerical noise

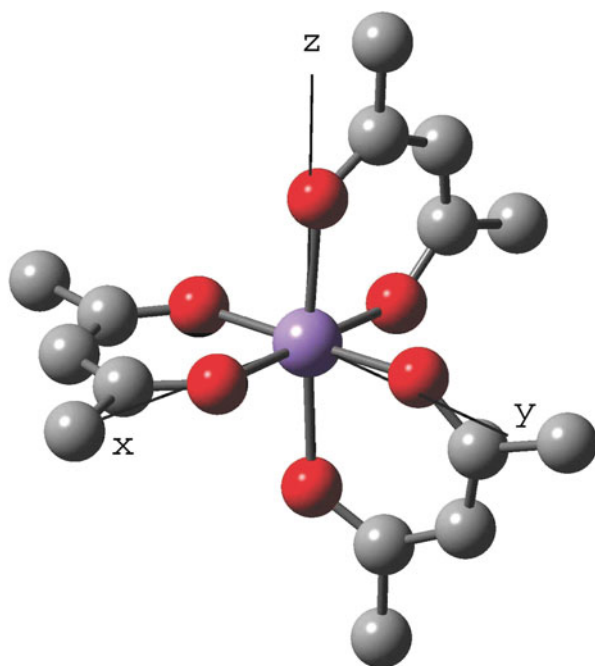
and do not significantly alter the extracted B_k^n values. Note that if one wants to neglect the B_4^n parameters, i.e., introduce only second-rank spin operators in the model Hamiltonian, as in $\widehat{H}_{\text{mod1}}$, it is important to check a priori that the $k = 4$ terms are not important to insure that the model and effective interaction matrices match. As will be discussed in section “[Magneto-Structural Correlations Based on Crystal-Field Models and Ab Initio Calculations](#)”, the fourth-rank Stevens parameters relate to the near-degeneracy of spin components of different SOF states. Therefore, one should not neglect them in such situations, as, for instance, in nearly octahedral manganese(III) complexes [45]. Note that, however, the Jahn-Teller effect tends to largely remove the near-degeneracy between the two lowest orbital configurations in this case, which explains, for instance, why the B_4^n parameters are not crucial to describe the ZFS in the $[\gamma\text{-Mn}(\text{acac})_3]$ (acac = acetylacetonato) complex (see Fig. 3) [49], for which the first coordination sphere is tetragonally elongated.

In many cases of experimental interest, $\widehat{H}_{\text{mod1}}$ is perfectly suited to describe the ZFS of $S = 2$ and $S = 5/2$ complexes.

Binuclear Complexes

Prior to introducing the model Hamiltonians that can be used to describe the ZFS in binuclear complexes, it is worth introducing the HDV Hamiltonian [19, 29, 88],

Fig. 3 Ball-and-stick representation of the $[\gamma\text{-Mn}(\text{acac})_3]$ complex and its main magnetic axes [49]. All the hydrogen atoms are omitted for clarity



which may be expressed in a “multispin” picture, i.e., by considering local spin operators that are to be applied within the basis of local spin components, i.e., within the uncoupled spin basis:

$$\widehat{H}_{\text{HDV}}^{\text{uncoupled}} = J \widehat{S}_a \cdot \widehat{S}_b$$

where J is the isotropic coupling constant and \widehat{S}_a and \widehat{S}_b are spin operator column vectors. Note that various expressions coexist in the literature, depending on a factor that is applied to this Hamiltonian (here 1, but one may find -1 or more often -2). It can easily be shown that $\widehat{H}_{\text{mod1}}$ can be also written in terms of spin operators that lead to a diagonal analytical interaction matrix if one works within the basis of spin eigenfunctions, i.e., within the coupled spin basis:

$$\widehat{H}_{\text{HDV}}^{\text{coupled}} = \frac{J}{2} \sum_S (\widehat{S}^2 - \widehat{S}_a^2 - \widehat{S}_b^2)$$

where S ranges between $|S_a - S_b|$ and $S_a + S_b$, \widehat{S} is the spin operator associated to each coupled spin state, and S_a and S_b are the local spins on the a and b sites. Therefore, it is clear that \widehat{H}_{HDV} splits the coupled spin states, which may further be the subject of ZFS and mixings when anisotropic effective interactions are considered in the model Hamiltonian. Such ZFSs and “spin mixings” can be effectively described in two different ways that work in the coupled and uncoupled basis, respectively, and which are classified as “giant-spin” or “block-spin” models and “multispin” ones.

Giant-Spin and Block-Spin Hamiltonians

If the isotropic coupling constantly plays a much more important role on the effective interaction matrix than the spin mixings, which is usually referred to as the “strong-exchange limit” [9], very simple models can be used to describe the low-energy spectrum. If only one spin “block” has to be described and that its magnetic axis frame is considered, one can use a very simple giant-spin Hamiltonian that is similar to $\widehat{H}_{\text{mod3}}$:

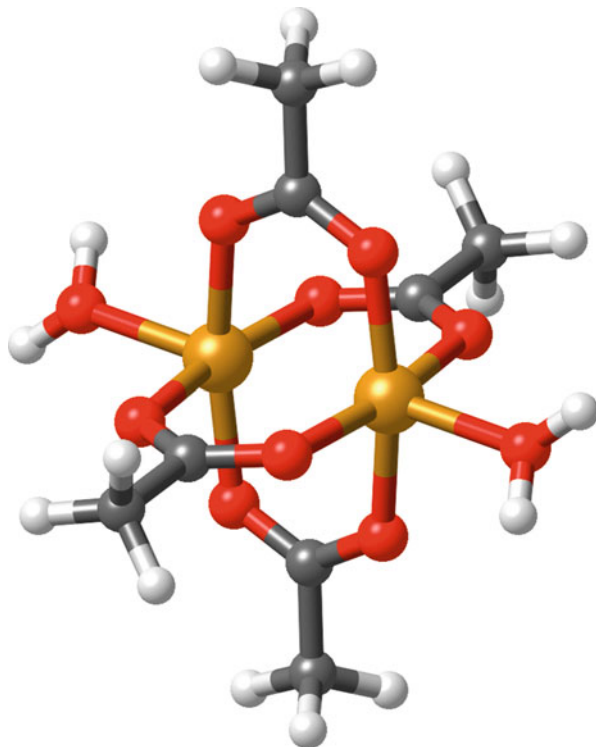
$$\widehat{H}_{\text{giant spin}}^{\text{coupled}} = \sum_{n=0}^k \sum_{k=2}^x B_k^n \widehat{O}_k^n$$

where $x = 2S$ if S is even or $x = 2S - 1$ if S is odd and k and n are even.

The simplest case is the ZFS of an $S = 1$ spin state resulting from the coupling of two local spins $S_a = S_b = 1/2$. One typical example of such a situation is copper acetate monohydrate (see Fig. 4) [50].

In this system, it is crucial to account for both SOC and SSC to compute the ZFS of the excited ${}^3A_{1u}$ SOF state. As shown by Maurice et al. [50], the treatment of SOC requires a special attention to the correlated energies appearing on the diagonal

Fig. 4 Ball-and-stick representation of copper acetate monohydrate [50]



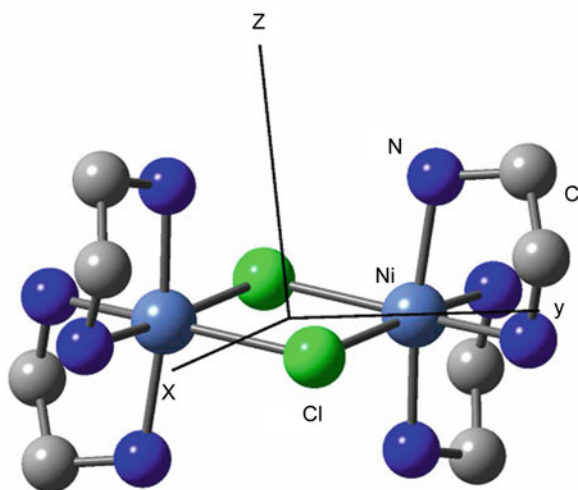
elements of the $\hat{H} = E_{el} + \hat{H}_{\text{SOC}} + \hat{H}_{\text{SSC}}$ matrix (see Table 3). The reference wave functions were obtained with SA-CASSCF(18/10) calculations (see [50] for more details). As can be seen in Table 3, second-order perturbation theory does not describe sufficiently well the SOF excitation energies, as well as variational approaches with limited configuration interaction spaces (the DDCI1 calculations include in this case only the $1h$ and $1p$ excitations, while the DDCI2 ones also account for the $1h1p$, $2h$, and $2p$ excitations). Although the DDCI2 level appears to lead to an almost converged value of D when only \hat{H}_{SOC} is considered, it is essentially due to error cancellations (more details are given on this in [50]). The best value, obtained with the DDCI3 energies, is in exceptional agreement with experiment ($D_{\text{expt.}} = -0.335 \text{ cm}^{-1}$ [65]). The rhombic E parameter value is very small, 0.006 cm^{-1} with the DDCI3 energies (in good agreement with $E_{\text{expt.}} = 0.01 \text{ cm}^{-1}$), and will not be discussed in details here.

One should stress that in this particular case, i.e. the d^9-d^9 configuration, computing the ZFS of the triplet block happened to be particularly challenging, but it may not be the case for other configurations. Another system that has been studied within the giant-spin approach is the $[\text{Ni}_2(\text{en})_4\text{Cl}_2]^{2+}$ (en = ethylenediamine) complex (see Fig. 5) [46, 47]. Although this system does not fall within the strong-exchange limit, it is possible to build two effective Hamiltonians in the basis of

Table 3 Computed axial ZFS D parameters as a function of the correlated energies used on the diagonal of the contracted configuration interaction matrices and of the operators introduced in the Hamiltonian [50]

E_{el}	\hat{H}_{SOC}	\hat{H}_{SSC}	$\hat{H}_{SOC} + \hat{H}_{SSC}$
SA-CASSCF	-0.017	-0.118	-0.137
NEVPT2	-0.026	-0.118	-0.144
DDCI1	0.005	-0.118	-0.115
DDCI2	-0.172	-0.118	-0.291
DDCI3	-0.200	-0.118	-0.319

Fig. 5 Ball-and-stick representation of the $[\text{Ni}_2(\text{en})_4\text{Cl}_2]^{2+}$ complex and its $S = 2$ block main magnetic axes. All the hydrogen atoms are omitted for clarity



the spin components of the $S = 2$, $S = 1$, and $S = 0$ spin components, one in which spin mixings are set to zero and one in which these spin mixings are allowed [47, 49]. From this theoretical study, it was shown that, in the magnetic axis frame, $\hat{H}_{\text{giantspin}}^{\text{coupled}}$ can describe the ZFS of both the $S = 2$ and $S = 1$ blocks in the absence of spin mixing and that the spin mixings can be described using additional operators [47] (in this case, due to a symmetry center, the spin mixings concern the $S = 0$ and some $S = 2$ spin components). In other words, one can define a block spin Hamiltonian which describes the isotropic coupling and the ZFSs of the different blocks in the absence of spin mixing, and the spin-mixing effects can actually be introduced inside the different spin blocks, i.e., one can use a block-diagonal analytical interaction matrix to describe the entire low-energy spectrum [49]. The comparison with experimental data is complicated since all the studies reported so far neglected some, and usually different, effective interactions in the model Hamiltonians [27, 30, 37, 38]. One can just mention that the best computed value for D_2 , i.e., the axial ZFS parameter of the $S = 2$ block, is in good semiquantitative agreement with the experimental one [30] (-3.0 vs. -1.8 cm^{-1} , respectively).

Table 4 Analytical interaction matrix corresponding to $\widehat{H}_{\text{multispin}}^{\text{uncoupled}}$ when $S_a = S_b = 1/2$ [48]. A shortened notation $|M_{S_a}, M_{S_b}\rangle$ is used for the $|S_b, M_{S_a}, S_b, M_{S_b}\rangle$ uncoupled functions. X , Y , and Z correspond to the Cartesian axes of an arbitrary axis frame

$\widehat{H}_{\text{multispin}}^{\text{uncoupled}}$	$ -1/2, -1/2\rangle$	$ -1/2, 1/2\rangle$	$ 1/2, -1/2\rangle$	$ 1/2, 1/2\rangle$
$\langle -1/2, -1/2 $	$\frac{1}{4}(J + T_{ZZ})$	$-\frac{1}{4}(T_{ZX} + iT_{ZY})$	$-\frac{1}{4}(T_{XZ} + iT_{YZ})$	$\frac{1}{4}[T_{XX} - T_{YY} + i(T_{XY} + T_{YX})]$
$\langle -1/2, 1/2 $	$-\frac{1}{4}(T_{ZX} - iT_{ZY})$	$-\frac{1}{4}(J + T_{ZZ})$	$\frac{1}{4}[2J + T_{XX} + T_{YY} + i(T_{YX} - T_{XY})]$	$\frac{1}{4}(T_{XZ} + iT_{YZ})$
$\langle 1/2, -1/2 $	$-\frac{1}{4}(T_{XZ} - iT_{YZ})$	$\frac{1}{4}[2J + T_{XX} + T_{YY} - i(T_{YX} - T_{XY})]$	$-\frac{1}{4}(J + T_{ZZ})$	$\frac{1}{4}(T_{ZX} + iT_{ZY})$
$\langle 1/2, 1/2 $	$\frac{1}{4}[T_{XX} - T_{YY} - i(T_{XY} + T_{YX})]$	$\frac{1}{4}(T_{XZ} - iT_{YZ})$	$\frac{1}{4}(T_{ZX} - iT_{ZY})$	$\frac{1}{4}(J + T_{zz})$

Another study of the d^8-d^8 configuration, related to the strong-exchange limit, concerned model complexes [74]. It was shown that, contrary to what is often proposed, no simple relations appear between the ZFS parameters of the $S = 2$ and $S = 1$ blocks, which can also be analyzed within a multispin picture (vide infra). Also, it is clear that giant-spin and block-spin Hamiltonians may not be relevant in the weak-exchange limit, i.e., when J becomes negligible, since spin mixings cannot be considered as a perturbation in such a case. In principle, one should in this case consider a multispin model, the extraction of which is far from being straightforward, as will be shown later.

Multispin Hamiltonians

As in section “[Mononuclear Complexes](#)”, we will introduce progressively the complexity of the multispin Hamiltonian in binuclear complexes. Let us start with the easiest case of two coupled $S = 1/2$ centers, as in the d^9-d^9 configurations, for instance. The model Hamiltonian which is commonly used includes an isotropic coupling terms (\widehat{H}_{HDV}) plus an anisotropy tensor [39]:

$$\widehat{H}_{\text{multispin}(S_a=S_b=1/2)}^{\text{uncoupled}} = J \hat{S}_a \cdot \hat{S}_b + \hat{S}_a \overline{\overline{T}}_{ab} \hat{S}_b = J \hat{S}_a \cdot \hat{S}_b + \hat{S}_a \overline{\overline{D}}_{ab} \hat{S}_b + \vec{d}_{ab} \hat{S}_a \times \hat{S}_b$$

where $\overline{\overline{T}}_{ab}$ is a second-rank tensor that is neither symmetric nor antisymmetric in the general case, $\overline{\overline{D}}_{ab}$ is the symmetric anisotropy exchange tensor, and \vec{d}_{ab} is the Dzyaloshinskii-Moriya term [22, 58] that can also be referred to as the antisymmetric exchange pseudo-vector. As mentioned earlier, computing $\overline{\overline{D}}_{ab}$ may turn into a real nightmare [50], but the semiquantitative determination of \vec{d}_{ab} is much less demanding, since it can be obtained from CASSCF(2/2) + c-SOCI calculations [48, 67]. The analytical interaction matrix built in the uncoupled basis is represented in Table 4.

One can also express this analytical interaction matrix with the $\overline{\overline{D}}_{ab}$ tensor and the \vec{d}_{ab} pseudo-vector by using the $D_{ii} = T_{ii}$, $D_{ij} = 1/2(T_{ij} + T_{ji})$, $d_X =$

$1/2(T_{YZ} - T_{ZY})$, $d_Y = 1/2(T_{ZX} - T_{XZ})$, and $d_Z = 1/2(T_{XY} - T_{YX})$ relations [48]. The analytical interaction matrix can be transformed into the coupled basis as follows:

$$\widehat{H}_{\text{multispin}}^{\text{coupled}} = U^T \widehat{H}_{\text{multispin}}^{\text{uncoupled}} U$$

where U^T is the transpose of the change of basis matrix U . The matrix elements of U are given by the appropriate Clebsch-Gordan coefficients [9]. When $\widehat{H}_{\text{multispin}}$ is expressed in the coupled basis, the $\overline{\overline{D}}_{ab}$ tensor relates to the splitting and mixing of the $S = 1$ block (i.e., its ZFS in the strong-exchange limit), while the \vec{d}_{ab} pseudo-vector introduces spin mixings between the $S = 1$ spin components and the $S = 0$ one. This type of S/S+1 spin mixing is not always symmetry allowed (the symmetry rules are available elsewhere [12]). One may just recall that if the system contains a symmetry center, as it is the case for copper acetate monohydrate, the \vec{d}_{ab} pseudo-vector is null [58]. Therefore, in this system, as in any other d^9-d^9 binuclear system, a simple relation appears between $\overline{\overline{D}}_1$ and $\overline{\overline{D}}_{ab}$ [50]:

$$\overline{\overline{D}}_1 = \frac{1}{2} \overline{\overline{D}}_{ab}$$

By studying model copper(II)-copper(II) complexes, Maurice et al. showed that $\widehat{H}_{\text{multispin}}$ is perfectly valid to describe the isotropic coupling and the ZFSs when $S_a = S_b = 1/2$ [48]. Owing to the effective Hamiltonian theory, all the model parameter values can be theoretically extracted, while it appears complicated to properly distinguish between the symmetric and antisymmetric exchange terms from the outcomes of experiments. Moreover, since one can obtain good semiquantitative estimates of the \vec{d}_{ab} pseudo-vector components from CASSCF(2/2)+c-SOCI calculations [48, 67], antisymmetric exchange is essentially due to the direct SOC between the $S = 1$ and $S = 0$ spin components.

When $S_a = 1$ and $S_b = 1/2$, another term must be added to the phenomenological model Hamiltonian, related to the single-ion anisotropy of site a [39]:

$$\widehat{H}_{\text{multispin}(S_a=1, S_b=1/2)}^{\text{uncoupled}} = J \hat{S}_a \cdot \hat{S}_b + \hat{S}_a \overline{\overline{D}}_a \hat{S}_a + \hat{S}_a \overline{\overline{D}}_{ab} \hat{S}_b + \vec{d}_{ab} \hat{S}_a \times \hat{S}_b$$

In this case, both the $\overline{\overline{D}}_a$ and $\overline{\overline{D}}_{ab}$ symmetric tensors affect the $S = 3/2$ block, while \vec{d}_{ab} relates to the S/S + 1 spin mixings, as usual.

The situation is drastically complicated when considering the $S_a = S_b = 1$ case, e.g. nickel(II)-nickel(II) complexes. The following model Hamiltonian was used for decades to interpret experimental data [27, 30, 37, 38]:

$$\widehat{H}_{\text{multispin}(S_a=S_b=1)}^{\text{uncoupled}} = J \hat{S}_a \cdot \hat{S}_b + \hat{S}_a \overline{\overline{D}}_a \hat{S}_a + \hat{S}_b \overline{\overline{D}}_b \hat{S}_b + \hat{S}_a \overline{\overline{D}}_{ab} \hat{S}_b + \vec{d}_{ab} \hat{S}_a \times \hat{S}_b$$

The validity of this model Hamiltonian was assessed by c-SOCI calculations and the effective Hamiltonian theory in 2010 by Maurice et al. [46]. It was shown that many terms of the effective interaction matrix which were obtained for the $[\text{Ni}_2(\text{en})_4\text{Cl}_2]^{2+}$ complex were not associated to any model parameter in the analytical interaction matrix. In order to reproduce all features of the effective Hamiltonian matrix, one must actually introduce a symmetric fourth-rank exchange tensor, \mathbf{D}_{aabb} , in the model Hamiltonian, leading to:

$$\begin{aligned} \widehat{H}_{\text{multispin}(S_a=S_b=1)}^{\text{uncoupled}} = & J \widehat{S}_a \cdot \widehat{S}_b + \widehat{S}_a \overline{\overline{D}}_a \widehat{S}_a + \widehat{S}_b \overline{\overline{D}}_b \widehat{S}_b + \widehat{S}_a \overline{\overline{D}}_{ab} \widehat{S}_b \\ & + \widehat{S}_a \otimes \widehat{S}_a \mathbf{D}_{aabb} \widehat{S}_b \otimes \widehat{S}_b \end{aligned}$$

if $\overline{\overline{d}}_{ab}$ is null. The extraction of the \mathbf{D}_{aabb} components is not straightforward even with all information contained in the 9×9 effective interaction matrix; one should thus consider relations between these components, as done in a study of model complexes [74]. One should thus stress that the spin mixings between the $S = 2$ and $S = 0$ spin components, mentioned in section “[Giant-Spin and Block-Spin Hamiltonians](#)”, can be interpreted in terms of the parameters of the multispin Hamiltonian after transforming the analytical interaction matrix to the coupled basis: these terms actually relate to all symmetric tensors of $\widehat{H}_{\text{multispin}}$, i.e., $\overline{\overline{D}}_a$, $\overline{\overline{D}}_b$, $\overline{\overline{D}}_{ab}$, and \mathbf{D}_{aabb} [47].

Another interesting point which is worth mentioning here is that one may be interested in computing only the local anisotropy tensors, i.e., $\overline{\overline{D}}_a$ and $\overline{\overline{D}}_b$. Various strategies exist; (i) one may replace one of the two magnetic centers by a model potential [46] or by a diamagnetic ion [11, 46, 53], (ii) one may also consider its lowest-energy closed-shell configuration [74], and (iii) another method considers local excitations while keeping the other site in its lowest-energy open-shell configuration [69]. This last strategy is meant to be the most accurate approach. From the study of model complexes, it was shown that the local anisotropy parameters that can be obtained in these various ways are in very close agreement with those obtained from the extraction of the interactions of $\widehat{H}_{\text{multispin}}$ [74]. In conclusion, if one wants to estimate local anisotropy parameters or local magnetic axes, these approaches can be safely considered. It is also worth mentioning here that in the general case, the $S/S + 1$ spin mixings do not arise solely from $\overline{\overline{d}}_{ab}$: the mismatch between the local magnetic axes of the local $\overline{\overline{D}}_a$ and $\overline{\overline{D}}_b$ tensors also affects the effective couplings related to these mixings. This can be easily shown by considering $D_a = D_b \neq 0$, $E_a = E_b = 0$, and an angle 2α between coplanar local $Z_{a,b}^m$ axes. If one builds the corresponding model interaction matrix within the uncoupled basis and transforms it to the coupled one, the $S/S + 1$ spin-mixing terms are found proportional to $D_a \sin 2\alpha$ (the details of the derivation are not given here for a sake of simplicity). It is thus clear that these terms vanish for $\alpha = 0$, as it is the case for centrosymmetric complexes. Therefore, the local anisotropy tensors can be affected in the general case by the $S/S + 2$ and to $S/S + 1$ spin mixings. Furthermore, note that one should also never neglect these terms within the weak-

exchange limit, contrary to what was done, for instance, to interpret the low-energy spectrum of a cobalt(II)-cobalt(II) complex [64]. From the perspective of modeling, it is not clear yet whether the model Hamiltonian used for the $S_a = S_b = 1$ case is directly applicable to any other configuration. Actually, higher-rank tensors could be necessary to reproduce all ZFS features for higher local spins [54], such as, for instance, a sixth-rank tensor in the $S_a = S_b = 3/2$ case.

Magneto-Structural Correlations

Magneto-structural correlations are particularly useful for chemists as they give clues to tune the properties of a system and pave the way for the rational design of new magnetic systems with predetermined properties. In the field of ZFS, they can be established from correlations of molecular geometry features with the experimental values of the parameters, as was done by Titiš and Boča in nickel(II) and cobalt(II) mononuclear complexes [84,85]. Here, we will only discuss magneto-structural correlations deduced from the analysis of ab initio results or from combined ab initio/crystal-field studies.

Magneto-Structural Correlations Based on Ab Initio Calculations

Due to the lack of intuition on the role of distortions on the \bar{d}_{ab} pseudo-vector components, Maurice et al. studied the effects of two angular distortions on the DM vector components on model $[\text{Cu}_2\text{O}(\text{H}_2\text{O})_6]^{2+}$ complexes (see Fig. 6) [48]. This study was based on CASSCF(2/2) + c-SOCI calculations and made use of the effective Hamiltonian theory, as mentioned in section “[Multispin Hamiltonians](#)”.

The norm of the \bar{d}_{ab} pseudo-vector as a function of the ϑ_1 and ϑ_2 deformation angles is represented in Fig. 7.

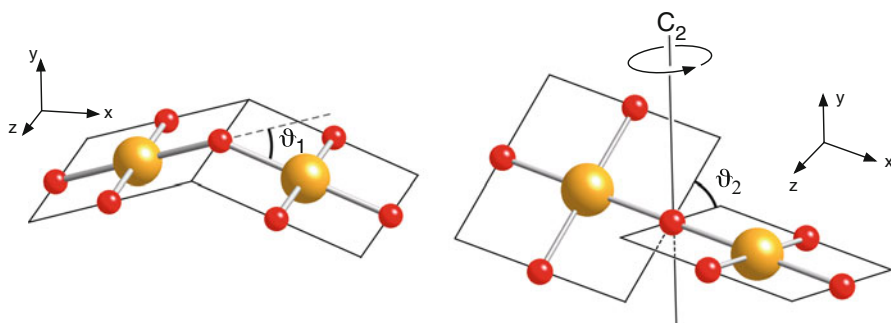


Fig. 6 Ball-and-stick representation of model $[\text{Cu}_2\text{O}(\text{H}_2\text{O})_6]^{2+}$ complexes and the deformation angles that were applied to them [48]. All the hydrogen atoms are omitted for clarity

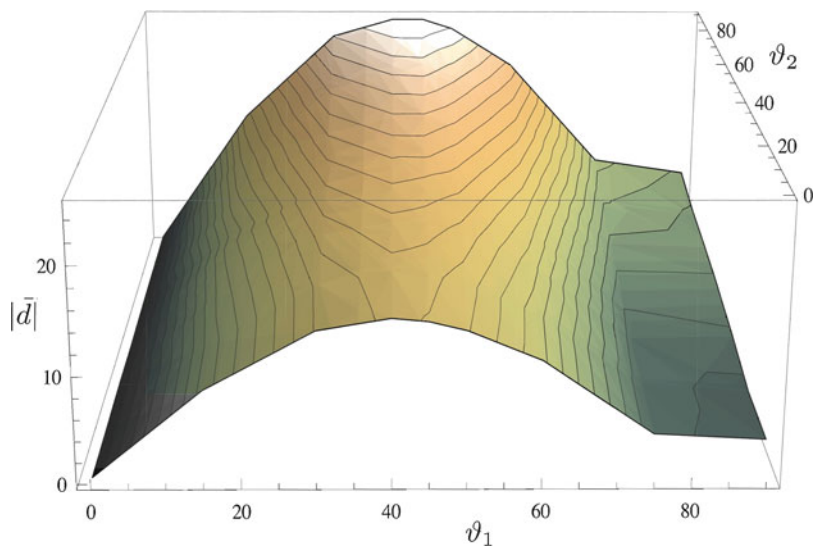


Fig. 7 Norm of the \bar{d}_{ab} pseudo-vector as a function of the ϑ_1 and ϑ_2 deformation angles (see Fig. 6 for the definition of these angles) [48]

In this study, the only point for which the \bar{d}_{ab} pseudo-vector is null by symmetry corresponds to the $\vartheta_1 = \vartheta_2 = 0$ case, for which the system possesses a symmetry center. Another interesting point refers to $\vartheta_1 = \pi/2$ and $\vartheta_2 = 0$. In this case, there is no atomic orbital contribution from the copper(II) centers, and as a consequence, the only important contribution to this norm comes from the bridging oxygen center. As the \bar{d}_{ab} pseudo-vector is far from being null, in this case ($|\bar{d}_{ab}| = 3.6 \text{ cm}^{-1}$ [48]) the (essentially) closed-shell bridging oxygen contributes to the norm of the \bar{d}_{ab} pseudo-vector, as highlighted by Moskvin in 2007 [59]. Other studies concerning single-ion anisotropies exist in the literature, among which one may quote the extensive one of Gomez-Coca et al. [28], but these will not be discussed here. Instead, we will explore the cases of mononuclear complexes for which ab initio calculations are used to extract crystal-field parameters.

Magneto-Structural Correlations Based on Crystal-Field Models and Ab Initio Calculations

Joint ab initio and crystal-field studies are important to validate the equations derived from the crystal-field theory and to interpret the outcomes of experiments in a simple way. It is commonly practiced on mononuclear complexes, although equations can also be derived in binuclear complexes, as was done, for instance, in the case of copper acetate monohydrate [50]. In this section, we shall illustrate the procedure for the d^8 and d^4 configurations, using ab initio calculations on nearly

octahedral $[\text{Ni}(\text{NCH})_6]^{2+}$ and $[\text{Mn}(\text{NCH})_6]^{3+}$ model complexes. In both cases, we define the axial deformation parameter as:

$$\tau_{ax} = \frac{2d(TM, N_Z)}{d(TM, N_X) + d(TM, N_Y)}$$

and the rhombic deformation as:

$$\tau_{rh} = \frac{d(TM, N_Y)}{d(TM, N_X)}$$

The mean $d(\text{TM}, \text{N})$ distance is 2.054 Å and 2.061 Å for $\text{TM}=\text{Ni}$ [49] and $\text{TM}=\text{Mn}$ [45], respectively, while all $d(\text{TM}, \text{C})$ parameters are fixed to 1.155 Å and all the $d(\text{C}, \text{H})$ ones to 1.083 Å. Minimal CASSCF calculations have been carried out with the five d-orbitals and 8 (Ni) or 5 (Mn) electrons within the active space. Note that in the formulae that are presented here, monoelectronic ζ SOC constants are considered. These constants are always positive and can be converted into polyelectronic λ ones by using the following relation:

$$\lambda = \pm \frac{\zeta}{2S}$$

where S is the total spin of the ground SOF free-ion multiplet.

It is easy to show, as done in the textbook of Abragam and Bleaney [1], that for axially distorted systems:

$$D = -\frac{\zeta^2}{\Delta_1} + \frac{\zeta^2}{\Delta_2}$$

where Δ_1 is the ${}^3\text{B}_{1g} \rightarrow {}^3\text{B}_{2g}$ excitation energy and Δ_2 corresponds to the ${}^3\text{B}_{1g} \rightarrow {}^3\text{E}_g$ excitation energy. The derivation of this equation is based on a model space containing the spin components of the ground SOF ${}^3\text{B}_{1g}$ state, while the external space consists of the spin components of the lowest two excited SOF states, namely, ${}^3\text{B}_{2g}$ and ${}^3\text{E}_g$, which are essentially singly excited states with respect to ${}^3\text{B}_{1g}$. To check the correlation between the ab initio results and the outcomes of the crystal-field model, we substitute the ab initio Δ_1 and Δ_2 values in the expression for D and take the SOC constant of the free Ni^{2+} ion, 648 cm^{-1} (see Table 5). As can be seen, a good correlation appears between the ab initio and the crystal-field D values (D_{CF}): the trend line that passes through the origin, as forced by symmetry, leads to $D_{CF} = 1.32 D$ with $R^2 = 0.9969$. This shows that accounting for covalency effects by applying a reduction factor of 0.87 brings the D_{CF} values in perfect agreement with the ab initio ones along the whole curve. Therefore, the crystal-field formula presented above is fully supported by c-SOCI calculations that consider the spin components of four SOF triplet states. Note that considering more SOF states in the first step of the calculation does not significantly improve the

Table 5 Ab initio Δ_1 , Δ_2 , and D values and values of D derived from the crystal-field expression (D_{CF}) obtained with $\zeta = 648 \text{ cm}^{-1}$ (all values are in cm^{-1}) [49]

τ_{ax}	Δ_1	Δ_2	D	D_{CF}
0.957	8382.4	9692.5	-5.519	-6.855
0.971	8669.7	9559.4	-3.568	-4.564
0.985	8964.0	9416.5	-1.736	-2.279
1.000	9266.9	9266.9	0.000	0.000
1.015	9576.9	9110.8	1.659	2.271
1.029	9895.8	8951.8	3.259	4.530
1.044	10,224.0	8791.1	4.814	6.778

computed values, meaning that this formula explains most of the ZFS in axially distorted six-coordinated nickel(II) complexes.

In a similar way, one can introduce a rhombic distortion, i.e., an in-plane radial distortion. The crystal-field derivation leads to:

$$D = -\frac{\zeta^2}{\Delta_1} + \frac{\zeta^2}{2\Delta_2} + \frac{\zeta^2}{2\Delta_3}$$

and:

$$E = -\frac{\zeta^2}{2\Delta_2} + \frac{\zeta^2}{2\Delta_3}$$

where Δ_1 correlates with the ${}^3B_{1g} \rightarrow {}^3B_{2g}$ energy difference in the D_{4h} symmetry point group and where Δ_2 and Δ_3 both correlate with the energy of the ${}^3B_{1g} \rightarrow {}^3E_g$ excitation in the same symmetry point group [49]. Similarly, it can be shown that these formulae are supported by ab initio calculations [49], corroborating that the outcomes of model complex studies which aim at establishing magneto-structural correlation can be safely explained by crystal-field models.

Before presenting the example of nearly octahedral manganese(III) complexes, it is worth mentioning that such derivations are only valid close to ideal geometries of high symmetry, since it is assumed that the ground and excited SOF wave functions are either (i) not much affected by the distortion or (ii) affected in a way that can be easily modeled. In general, it is always advisable to perform ab initio calculations and to analyze the nature of the SOF wave functions of interest. For instance, large angular distortions usually result in a mixing of various configurations in such a complex way that pen-and-paper analytical derivations become cumbersome. Moreover, even if analytical derivations can be performed, if the resulting formulae are too complicated, they become pointless in practice for establishing or understanding magneto-structural correlations. In such cases, it is preferable to directly establish the correlations by means of ab initio calculations, as presented in section “[Magneto-Structural Correlations Based on Ab Initio Calculations](#)”.

Another interesting point concerns the role of the second coordination sphere. Although this effect is traditionally neglected in crystal-field models, it was shown

Table 6 Analytical crystal-field expressions of the energies, ab initio, and derived crystal-field energies (in cm^{-1}) [45]. For the computation of the crystal-field energies, the free-ion SOC of 352 cm^{-1} and ab initio SOF excitation energies of $\Delta Q = 13,993 \text{ cm}^{-1}$ and $\Delta T = 11,005 \text{ cm}^{-1}$ have been used

Multiplicity	$E_{\text{analytical}}$	$E_{\text{ab initio}}$	E_{CF}
Singlet	$2 \frac{4\Delta Q\zeta^2 + 3\Delta T\zeta^2}{8\Delta Q\Delta T}$	16.813	17.900
Triplet	$\frac{4\Delta Q\zeta^2 + 3\Delta T\zeta^2}{8\Delta Q\Delta T}$	8.399	8.950
Doublet	0	0.000	0.000
Triplet	$-\frac{4\Delta Q\zeta^2 + 3\Delta T\zeta^2}{8\Delta Q\Delta T}$	-8.890	-8.950
Singlet	$-2 \frac{4\Delta Q\zeta^2 + 3\Delta T\zeta^2}{8\Delta Q\Delta T}$	-17.775	-17.900

by means of ab initio calculations that the second coordination sphere can play a crucial role on the single-ion anisotropy in some particular cases [11, 51].

Nearly octahedral manganese(III) complexes, corresponding to the d^4 configuration, are particularly interesting as they present nonintuitive ZFSs [45]. Although formulae which rationalize the ZFS of such systems are presented in the book of Abragam and Bleaney [1], this case is often misinterpreted. Ab initio calculations showed that the external space cannot be restricted to quintet-spin SOF state components. Indeed, three triplet-spin roots must also be included in the derivation to obtain accurate crystal-field formulae for this configuration [45]. The use of these newly derived expressions leads to the energies of the ten spin components of the SOF 5E state reported in Table 6. Note that the same wave functions as those obtained by Abragam and Bleaney with five quintet roots were obtained [1]. The trend line $E_{CF} = 1.034 E_{\text{ab initio}}$ has an R^2 value of 0.9992, meaning that (i) the crystal-field formulae presented in Table 6 are valid and (ii) a reduced effective SOC constant of 346 cm^{-1} has to be used in the crystal-field model to effectively account for covalency.

Similarly to the nickel(II) case, one can derive formulae for the D and E parameters of Mn(III) complexes which belong to the D_{4h} and D_{2h} symmetry point groups. In this case, analytical formulae can also be written down for the parameters appearing in the Stevens fourth-rank operators. However, as shown in [45], one can consider various approximations, i.e., neglecting (i) the Stevens fourth-rank terms (large distortions) and (ii) the degeneracy lift of the excited SOF multiplets of the octahedral situation (${}^3T_{1g}$ and ${}^5T_{2g}$). For the former approximation, one should note that in the case of small distortions, the Stevens fourth-rank terms can be important as they are closely related to the near-degeneracy of the states that originate from the 5E_g of the octahedron [45]. In the D_{2h} symmetry point group, two configurations mix to form the two lowest SOF states [1]. It is therefore necessary to introduce a mixing parameter δ to express these states as:

$$|\phi_1\rangle = \cos \delta |Q_1\rangle + \sin \delta |Q_2\rangle$$

and:

$$|\phi_2\rangle = -\sin \delta |Q_1\rangle + \cos \delta |Q_2\rangle$$

where Q_1 and Q_2 are the two coupled configurations. This leads, after some pen-and-paper work, to [45]:

$$D = \zeta^2 \cos 2\delta \left[\frac{3}{16\Delta Q} + \frac{1}{4\Delta T} \right]$$

and:

$$E = \zeta^2 |\sin 2\delta| \left[\frac{3}{16\Delta Q} + \frac{1}{4\Delta T} \right]$$

where E is defined positive by convention. The careful reader will notice that, as in the octahedral situation, the contribution of the triplet roots which were added in this derivation is proportional to the effect of the quintet roots that correlate with ${}^5T_{2g}$ in the octahedron. Finally, we end up with the same formula as the one reported in the book of Abragam and Bleaney [1]:

$$\frac{E}{|D|} = \frac{\sqrt{3}}{3} |\tan 2\delta|$$

To conclude, one should mention that the anisotropy parameters are not enlarged by distorting the first coordination sphere in this configuration, as illustrated by Fig. 8 in the case of axial distortions. The ZFS of complexes belonging to this configuration is nonintuitive, and the combined ab initio and crystal-field model study has proved to be enlightening for experimental applications. Indeed, in this configuration, it is pointless to synthesize complexes with large distortions to enlarge the ZFS parameters, which is notably consistent with the empirical fact that d^4 complexes typically have axial ZFS parameter values ranging between -5 and 5 cm^{-1} [10].

Conclusion

In this chapter, we have shown that phenomenological Hamiltonians can be justified or even improved using the effective Hamiltonian theory; this creates a bridge between (supposedly) accurate ab initio calculations and intuitive models. We have also exemplified how the crystal-field theory can be used to rationalize the nature and magnitude of ZFS. These tools allow us to take another step in the direction of the control of magnetic properties as they provide concrete understanding of how to increase the magnetic anisotropy. Magneto-structural correlations have also been established, which may help to design molecules with desired properties. To

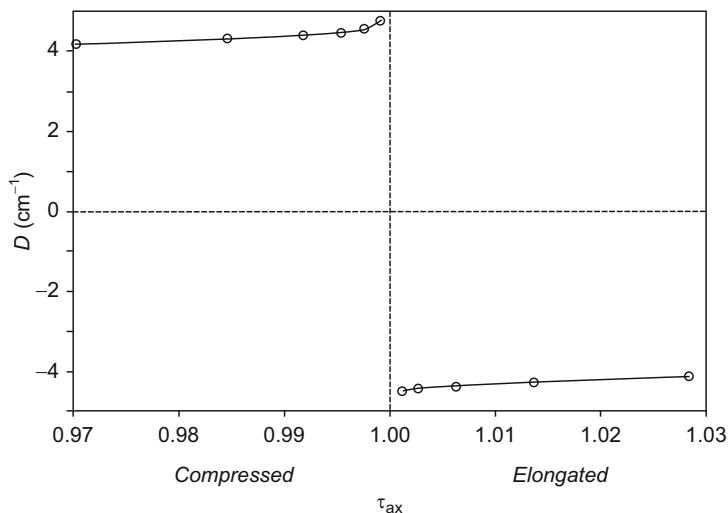


Fig. 8 Ab initio D parameter as a function of the axial distortion in model D_{4h} manganese(III) complexes [45]

maximize single-ion anisotropies, researchers followed strategies such as exploring exotic coordination spheres (for instance, pentacoordinate or heptacoordinate complexes) and even low-coordination spheres. Several efforts have been devoted to binuclear and polynuclear systems, more often concerning single-ion anisotropies but also concerning giant-spin and multispin models. Consequently, substantial progress has been made in the understanding of the magnitude and nature of the magnetic anisotropy in TM complexes with a wide range of ZFS parameter values over the last two decades.

Nevertheless, many aspects deserve further studies. For instance, the treatment of large systems is still problematic as (i) it is not clear which method can be used to obtain an optimal balance between accuracy and efficiency and (ii) current models to describe polynuclear complexes may not be complete. Indeed, even in the case of mononuclear complexes, some cases are typically pathological, e.g., when heavy atom ligands are involved. In this situation, it is not clear yet if sum-over-states or c -SOC approaches can be safely applied to the computation of the ZFS due to the truncation and state-averaging errors [49]. One may thus prefer to introduce the spin-dependent effects a priori, as done within $2c$ frameworks. Also, some experimental data may have been incorrectly interpreted due to the use of inadequate models to fit the experimental outcomes of various techniques (magnetic susceptibility, magnetization, EPR, etc.). Therefore, there is clearly a need for more extensive studies and developments in the field of molecular magnetism. We hope that this chapter will motivate future work of this kind.

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